

ECE2020 Test 1 Summer 2013 GTL

May 31, 2013

Name: _____

5 pages, 100 possible points. **Show your work for any possible partial credit.**

Switch level circuits:

1) (15 total point) For the expression below, create a switch level implementation using N and P type switches. Assume both inputs and their complements are available. Your design should contain no shorts or floats. Implement the equations exactly as they are (no simplifying).

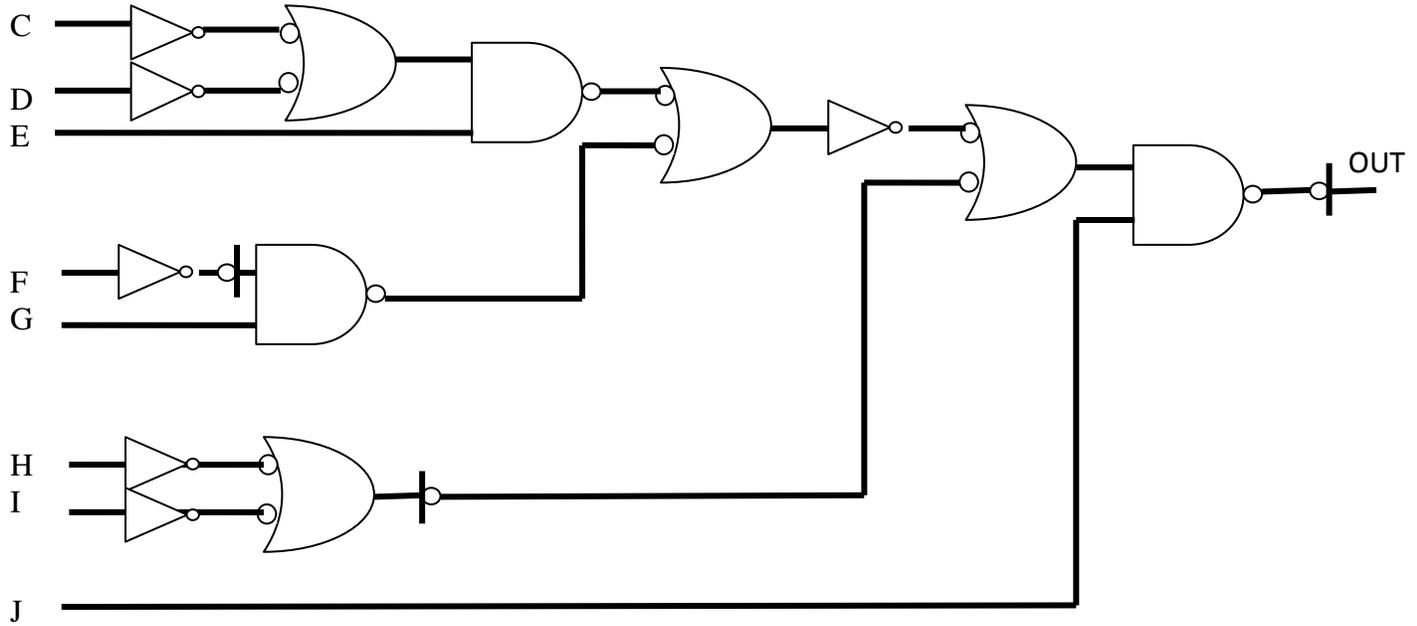
$$\text{Out}_x = (C + \overline{D}) \cdot (E + F) \cdot \overline{A} \cdot B$$

Switch-Ready Expressions:

2) (15 points) Transform each of the following Boolean expressions to a form where they are ready for switch level implementation (i.e., there should only be bars over input variables, not over operations). The behavior of the expression should remain unchanged. **Do not implement**, just show the new Boolean equation without any "big bars".

$$\text{Outx} = \overline{(A + B)} (C + D) \overline{(E + F)}$$

3) Part A (15 points) Write the boolean output expression for the gate design shown below. Also determine the number of switches used in its implementation.



Out _____

number of switches _____

3) Part B (15 points) Implement the following expression using only two input OR gates and inverters so as to minimize the number of switches required. Then determine the number of switches required. Use **proper mixed logic notation**. Do not modify the expression, do not simplify the expression. Do not assume complements of inputs are available.

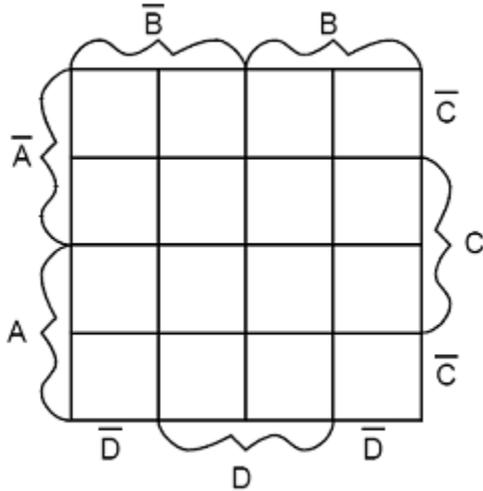
$$\text{Out} = \overline{(\overline{A + B + C}) \cdot \overline{D} + \overline{EF}} \cdot G$$

Number of switches _____

Karnaugh Maps:

4) (15 points) For the following expression, derive a simplified *sum of products* expression using a Karnaugh Map. Circle and list **ALL** the prime implicants, indicating which are essential.

$$A \cdot \overline{C} + A \cdot B \cdot \overline{C} + B \cdot \overline{D} + B \cdot C \cdot D$$



prime implicants	essential?	
	yes	no
_____	<input type="checkbox"/>	<input type="checkbox"/>
_____	<input type="checkbox"/>	<input type="checkbox"/>
_____	<input type="checkbox"/>	<input type="checkbox"/>
_____	<input type="checkbox"/>	<input type="checkbox"/>
_____	<input type="checkbox"/>	<input type="checkbox"/>
_____	<input type="checkbox"/>	<input type="checkbox"/>
_____	<input type="checkbox"/>	<input type="checkbox"/>
_____	<input type="checkbox"/>	<input type="checkbox"/>

Simplified sum of products _____

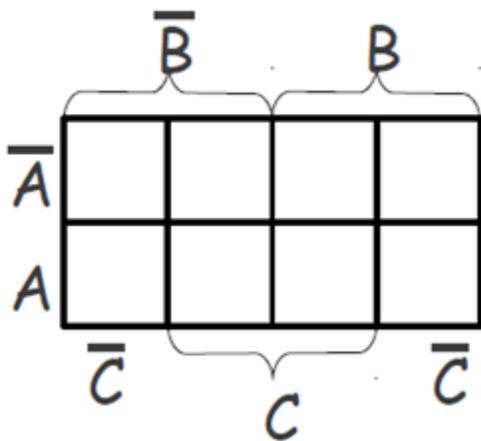
5) (10 points) Determine the canonical product of sums (using maxterms) expressions for the truth table below:

A	B	C	OUT
0	0	0	1
0	0	1	1
0	1	0	1
0	1	1	1
1	0	0	0
1	0	1	0
1	1	0	0
1	1	1	0

POS (maxterms) = _____

6) (15 points) For the following expression, derive a simplified *product of sums* expression using a Karnaugh Map. Circle and list **ALL** the prime implicants, indicating which are essential.

$$\text{out} = (A+B+C) (A+\bar{B}+C) (A+B+\bar{C}) (\bar{A} + \bar{B} + \bar{C}) (\bar{A} + B + \bar{C})$$



prime implicants	essential?	
	yes	no
_____	<input type="checkbox"/>	<input type="checkbox"/>
_____	<input type="checkbox"/>	<input type="checkbox"/>
_____	<input type="checkbox"/>	<input type="checkbox"/>
_____	<input type="checkbox"/>	<input type="checkbox"/>
_____	<input type="checkbox"/>	<input type="checkbox"/>

Simplified product of sums = _____