

Instructions: This is a closed book, closed note exam. Calculators are not permitted. If you have a question, raise your hand and I will come to you. Please work the exam in pencil and do not separate the pages of the exam. For maximum credit, show your work.
Good Luck!

Your Name (*please print*) _____

1	2	3	4	total
22	28	24	26	100

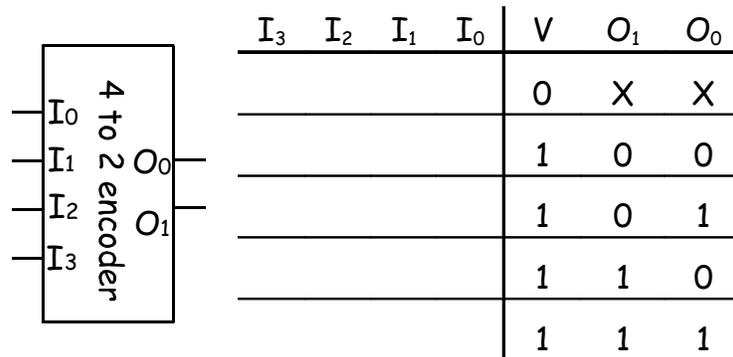


Problem 1 (3 parts, 22 points)

Building Blocks

Part A (6 points) Implement a 1 to 2 demultiplexor with pass gates and inverters. Be sure to label all inputs and outputs.

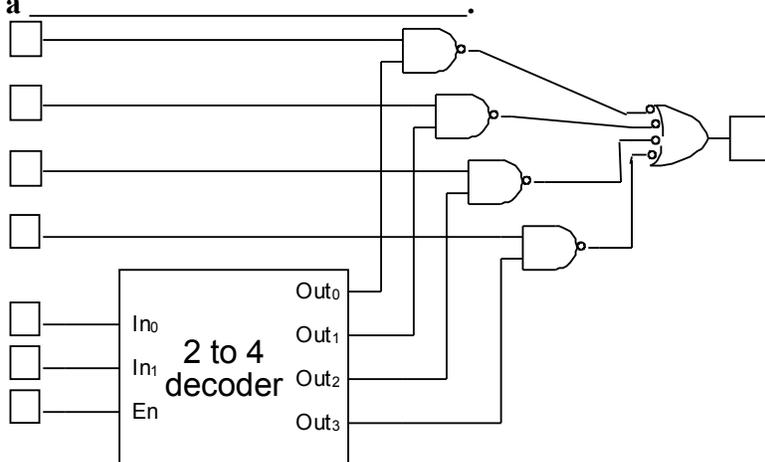
Part B (8 points) Suppose the circuit below has the following input priority: $I_2 > I_3 > I_0 > I_1$. Complete the truth table by filling in the input values that would produce the given outputs and derive a simplified expression for O_1 .



$O_1 =$ _____

Part C (8 points) Which building block does the following circuit implement? Label all inputs and outputs by filling in the squares.

This implements a _____.



Problem 2 (3 parts, 28 points)

Number Systems

Part A (10 points) Convert the following notations:

binary notation	decimal notation
1010 1100.	
	6.6875
101 1111.101	
hexadecimal notation	octal notation
	243.54
5F3.DC	

Part B (12 points) For the 32 bit representations below, determine the most positive value and the step size (difference between sequential values). **All answers should be expressed in decimal notation.** Fractions (e.g., 3/16ths) may be used. Signed representations are two's complement.

representation	most positive value	step size
unsigned integer (32 bits) . (0 bits)		
signed fixed-point (24 bits) . (8 bits)		
signed fixed-point (28 bits) . (4 bits)		
signed fixed-point (16 bits) . (16 bits)		

Part C (6 points) A 24 bit floating point representation has a 15 bit mantissa field, a 8 bit exponent field, and one sign bit.

What is the largest value that can be represented (closest to infinity)? **2** _____

What is the smallest value that can be represented (closest to zero)? **2** _____

How many decimal significant figures are supported? _____

Problem 3 (3 parts, 24 points)

Adding & Subtracting

Part A (12 points) For each problem below, compute the operations using the rules of arithmetic, and indicate whether an overflow occurs assuming all numbers are expressed using a **six bit unsigned** and **six bit two's complement** representations.

$$\begin{array}{r}
 101101 \\
 + 10111 \\
 \hline
 \end{array}
 \qquad
 \begin{array}{r}
 1110 \\
 + 10101 \\
 \hline
 \end{array}
 \qquad
 \begin{array}{r}
 11001 \\
 - 111000 \\
 \hline
 \end{array}
 \qquad
 \begin{array}{r}
 110100 \\
 - 10010 \\
 \hline
 \end{array}$$

result

 unsigned
error?

 signed
error?

Part B (4 points) Complete the truth table below for a full adder.

A	B	C _{in}	C _{out}	Sum
0	0	0		
0	0	1		
0	1	0		
0	1	1		
1	0	0		
1	0	1		
1	1	0		
1	1	1		

Part C (8 points) Implement the full adder using only NAND, XOR, and inverter gates. Label inputs **A**, **B**, and **C_{in}**. Label outputs **C_{out}** and **Sum**.

Problem 4 (4 parts, 26 points)

Registers and Latches

Part A (6 points) Implement a transparent latch using gates of any type (e.g., AND, inverter, pass gates), but use the minimum number of transistors. Label the inputs **In** and **En**, and output **Out**.

Part B (7 points) Design an RS latch using NOR gates only. Label inputs R and S. Label outputs OUT and $\overline{\text{OUT}}$. Do not attempt to employ mixed logic notation. Also complete the truth table.

R ———

————— Out

S ———

————— $\overline{\text{Out}}$

R	S	OUT	$\overline{\text{OUT}}$
0	0		
0	1		
1	0		
1	1		

Part C (5 points) Expand the RS latch to an implementation of a two-phase non-overlapping clock, generated from an input signal **In** that is a periodic square wave. Use only an RS latch and basic gates (AND, OR, NAND, NOR, and inverters). Label the input **In** and the outputs F1 and F2.

Part D (8 points) Assume the following signals are applied to a register with write enable. Draw the output signal **Out**. Draw a vertical line where **In** is sampled. Assume **Out** is initially zero.

