

## ECE2020 A Fall 2018 Test 1

Name: \_\_\_\_\_

- Only a writing implement may be used on this exam (i.e. no books, notes, or any electronics).
- If the meaning of any question is not clear, please ask for clarification.
- Partial credit can only be awarded for work shown.

### Honor pledge:

*On my honor, I pledge that I will neither receive nor provide improper assistance in the completion of this test. I understand and accept my responsibility as a member of the Georgia Tech Community to uphold the Honor Code at all times, and I know that I have options for reporting honor violations at [osi.gatech.edu](http://osi.gatech.edu).*

GTID: \_\_\_\_\_

Signature: \_\_\_\_\_

### Boolean Identities

|                       |   |  |
|-----------------------|---|--|
| Identity              | $A + 0 = A$   | $A \cdot 1 = A$                              |
| Dominance             | $A + 1 = 1$   | $A \cdot 0 = 0$                              |
| Idempotence           | $A + A = A$   | $A \cdot A = A$                              |
| Inverse               | $A + \bar{A} = 1$   | $A \cdot \bar{A} = 0$                        |
| Commutative           | $A + B = B + A$   | $A \cdot B = B \cdot A$                      |
| Associative           | $A + (B + C) = (A + B) + C$   | $A \cdot (B \cdot C) = (A \cdot B) \cdot C$  |
| Distributive          | $A \cdot (B + C) = A \cdot B + A \cdot C$                               | $A + B \cdot C = (A + B) \cdot (A + C)$      |
| Absorption            | $A \cdot (A + B) = A$   | $A + A \cdot B = A$                          |
| DeMorgan's            | $\overline{(A + B)} = \bar{A} \cdot \bar{B}$                            | $\overline{(A \cdot B)} = \bar{A} + \bar{B}$ |
| Double Complement     | $\bar{\bar{A}} = A$   |  |
| FOIL                  | $(A + B) \cdot (C + D) = A \cdot C + A \cdot D + B \cdot C + B \cdot D$ |  |
| Disappearing opposite | $A + \bar{A} \cdot B = A + B$   |  |

**This page is for scratch work and will not be graded unless you tell me that something on here needs to be graded.**

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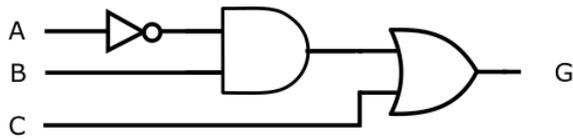
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| 1 | 0 | 1 | 0 |  |
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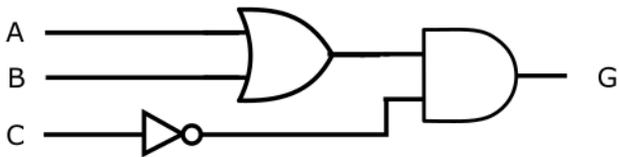
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| 0 | 0 | 0 | 0 |  |
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| 0 | 1 | 1 | 0 |  |
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| 1 | 0 | 0 | 0 |  |
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**Problem 1:** (20 points)

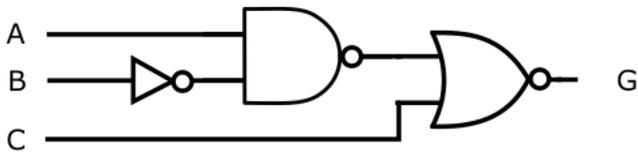
Write a Boolean expression for each of these gate schematics.



G = \_\_\_\_\_



G = \_\_\_\_\_



G = \_\_\_\_\_

**Problem 2:** (10 points)

A design team created the following logic expression for a project:

$$X = \overline{\overline{A + B \cdot C} + A \cdot D \cdot \overline{E}} + F \cdot G$$

That logic is correct, but at the last minute, the customer added a new requirement:

“Add a new input H. If H is low, output X must be low, otherwise use the same logic as before”

Make the simplest change possible to add the required behavior. You’re welcome to either write a new expression, or just describe what you would do.

**Problem 3:** (25 points)

Implement the following Boolean expression in proper CMOS (N-FETs and P-FETs). Assume that inputs and their complements are available (i.e. you may use something like  $\bar{C}$  as an input to a FET if needed).

$$F = \overline{(\bar{A} \cdot (\bar{B} + C))} + D$$

Derive expressions for the pull-up and pull-down switch networks (p.u. and p.d.) here:

Draw CMOS here:

p.u. = \_\_\_\_\_

p.d. = \_\_\_\_\_



**Problem 5:** (25 points)

Using the truth table below, create a K-map and solve for a minimal sum-of-products expression.

| A | B | C | D | Y |
|---|---|---|---|---|
| 0 | 0 | 0 | 0 | 0 |
| 0 | 0 | 0 | 1 | 0 |
| 0 | 0 | 1 | 0 | 1 |
| 0 | 0 | 1 | 1 | 0 |
| 0 | 1 | 0 | 0 | 1 |
| 0 | 1 | 0 | 1 | 0 |
| 0 | 1 | 1 | 0 | 1 |
| 0 | 1 | 1 | 1 | 0 |
| 1 | 0 | 0 | 0 | 1 |
| 1 | 0 | 0 | 1 | 0 |
| 1 | 0 | 1 | 0 | 1 |
| 1 | 0 | 1 | 1 | 0 |
| 1 | 1 | 0 | 0 | 1 |
| 1 | 1 | 0 | 1 | 1 |
| 1 | 1 | 1 | 0 | 1 |
| 1 | 1 | 1 | 1 | 1 |

Label the rows and columns of the K-map appropriately.

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**Y =** \_\_\_\_\_